## Midterm Physics 9B fall 2001

Use a law blue book. Closed book. One 3"x5" note card. PRINT your name on your blue book. To get credit, you must show your work. Be neat, clear, and organized. If we can't read it or figure it out, we can't give you any points. I am sure that none of you want to grow up to be like the person who sent the Mars Climate Orbiter to its death. Thus give the units for your answers. You will lose points for an answer with incorrect units.

1) (20 points) Consider a string which is infinitely long in both directions and on which the wave speed is $10 \mathrm{~m} / \mathrm{s}$. Which of the following functions describe possible motions of the string? Answer yes or no for each and give your reasoning or a direct calculation.
a) $y(x, t)=(5 \mathrm{~cm}) \sin (50 t / s-4 x / m)$
b) $y(x, t)=(2 \mathrm{~cm}) \cos (50 t / s+5 x / m)$
c) $y(x, t)=(3 \mathrm{~cm}) \cos (10 \mathrm{t} / \mathrm{s}) \sin (\mathrm{x} / \mathrm{m})$
d) $y(x, t)=(10 \mathrm{~cm}) /\left[2+(x / m-10 t / s)^{2}\right]$
2) ( 15 points) A string with clamped ends has a normal mode with frequency 10 Hz . (In the following, explain any that you select. You need not explain those that you do not select.)
a) Which of the following are definitely other normal mode frequencies? $5 \mathrm{~Hz}, 20 \mathrm{~Hz}, 30 \mathrm{~Hz}, 35 \mathrm{~Hz}$.
b) Which of the following could be the frequencies of other normal modes? $5 \mathrm{~Hz}, 15 \mathrm{~Hz}, \pi \mathrm{~Hz}, \sqrt{ } 2 \mathrm{~Hz}$.
c) Which of the following are definitely not the frequencies of other normal modes? $5 \mathrm{~Hz}, 15 \mathrm{~Hz}, \mathrm{\pi Hz}, \sqrt{ } 2 \mathrm{~Hz}$.
3) (15 points) Consider the standing wave $\mathrm{y}(\mathrm{x}, \mathrm{t})=(2 \mathrm{~cm}) \sin (3 \pi \mathrm{vt} / \mathrm{L}) \sin (3 \pi \mathrm{x} / \mathrm{L})$ on a string clamped at $\mathrm{x}=0$ and $\mathrm{x}=\mathrm{L}$ and on which waves travel with speed $v$.
a) Sketch the string at $\mathrm{t}=0$.
b) Sketch the string at $\mathrm{t}=\mathrm{L} /(6 \mathrm{v})$.
c) Compute $v_{y}(x)=\partial y(x, t) / \partial t$ at $t=0$ and $t=L /(6 v)$.
d) The conservation of energy demands that the energies in the string at $\mathrm{t}=0$ and $\mathrm{t}=\mathrm{L} /(6 \mathrm{v})$ are equal. Using your results from $\mathrm{a}, \mathrm{b}$, and c , explain in a qualitative way how that could be true.

4) (20 points) Three coherent sources are arranged as drawn. There is a principle maximum with intensity $\mathrm{I}_{0}$ at $\theta=0$.
a) What are the directions $\theta_{1}$ and $\theta_{2}$ to the next two principle maxima with intensity $\mathrm{I}_{0}$ ? $\left(0<\theta_{1}<\theta_{2}\right)$
b) In terms of $I_{0}$, what is the intensity at $\theta_{1} / 2$ ?
5) (15 points) a) In a laboratory experiment on earth, a certain kind of atom produces a particular characteristic wavelength of light. That light makes an intensity pattern when it passes through a slit 0.1 mm wide. The first minimum of the pattern is 0.6 cm from central maximum on a screen 1 m from the slit. What is the wavelength of the light?
b) A long time ago in a galaxy far, far away, the same kind of atoms emitted light with the same characteristic wavelength. However when the light arrives at earth and passes through the slit, the first minimum is farther from the central maximum. What qualitative statement can you make about the motion of the galaxy? Explain.
6) (15 points) Two speakers are driven in phase by the same 2 kHz signal. They are separated by 1 m . You are standing on the centerline 20 m from the speakers.


In that position, the sound intensity is $\mathrm{I}_{0}$. If you step 1 m off the centerline, by what factor does the sound intensity decrease? Use $300 \mathrm{~m} / \mathrm{s}$ for the speed of sound.

