

Step potential summary

This is a summary of the *results* of the calculation for the step potential done in class. It is *not* intended to be the complete calculation or to be a substitute for the full discussion. It is supposed to be enough of the results that you can check yourself and reproduce other things you might want or need.

$V(x)=0$ for $x<0$ and $V(x)=V_0$ for $x>0$.

To the left of $x=0$, $\psi_{EL}(x) = ae^{ipx/\hbar} + be^{-ipx/\hbar}$

and to the right $\psi_{ER}(x) = ce^{iqx/\hbar}$ with $p^2=2mE$ and $q^2=2m(E-V_0)$.

The boundary conditions at $x=0$ are $\psi_{EL}(0) = \psi_{ER}(0)$ and $\psi'_{EL}(0) = \psi'_{ER}(0)$

After some calculation, I got $b = a \frac{p-q}{p+q}$ and $c = a \frac{2p}{p+q}$.

In the case that $E-V_0 < 0$, q is imaginary, and the $x>0$ form is $\psi_{ER}(x) = ce^{-\sqrt{2m(V_0-E)} x/\hbar}$.

The quantum fluxes are important physical quantities. The flux is the density times the velocity. So the flux on the left heading right is $p|a|^2/m$. The flux on the left heading left is $p|b|^2/m$. The flux on the right heading right is $q|c|^2/m$.